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# **Robust Transmission over Fast Fading Channels on the Basis of OFDM-MFSK**

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## Outline

- ◆ Motivation
- ◆ A Robust Transmission Scheme – OFDM-MFSK
- ◆ Increasing the Bandwidth Efficiency using Hybrid Modulation
- ◆ BER Simulation Results
- ◆ The PAPR Problem
- ◆ PAPR Reduction Methods
- ◆ Conclusions



## Motivation

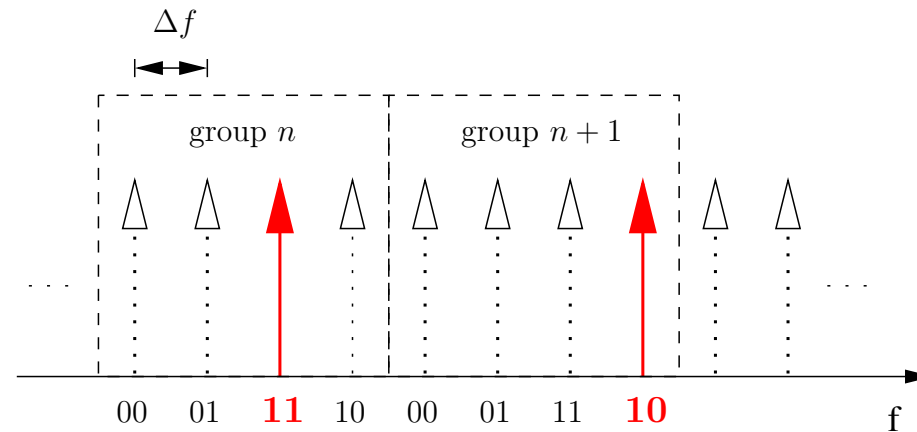
- ◆ Scenario: Communication with high speed trains
- ◆ Speed up to 600 km/h causes fast changing channels
- ◆ Channel estimation is very difficult
- ◆ Security relevant control data requires robust transmission
- ◆ Additional services for passengers like internet access require high data rates
- ◆ FSK schemes are very robust and are currently in use



**Goal:** Robust transmission scheme based on OFDM with high data rate



## A Robust Transmission Scheme – OFDM-MFSK



- ◆ Subcarriers are grouped into groups of  $M$  and MFSK modulation is applied to each group
- ◆ Alternative: Multitone FSK ( $N$  out of  $M$  subcarriers occupied)
- ◆ No CSI is needed for noncoherent detection
- ◆ Very robust against time variant channels
- ◆ Low bandwidth efficiency (uncoded OFDM-4FSK: 0.5 bit/subcarrier)



## A Robust Transmission Scheme – OFDM-MFSK

Noncoherent detection

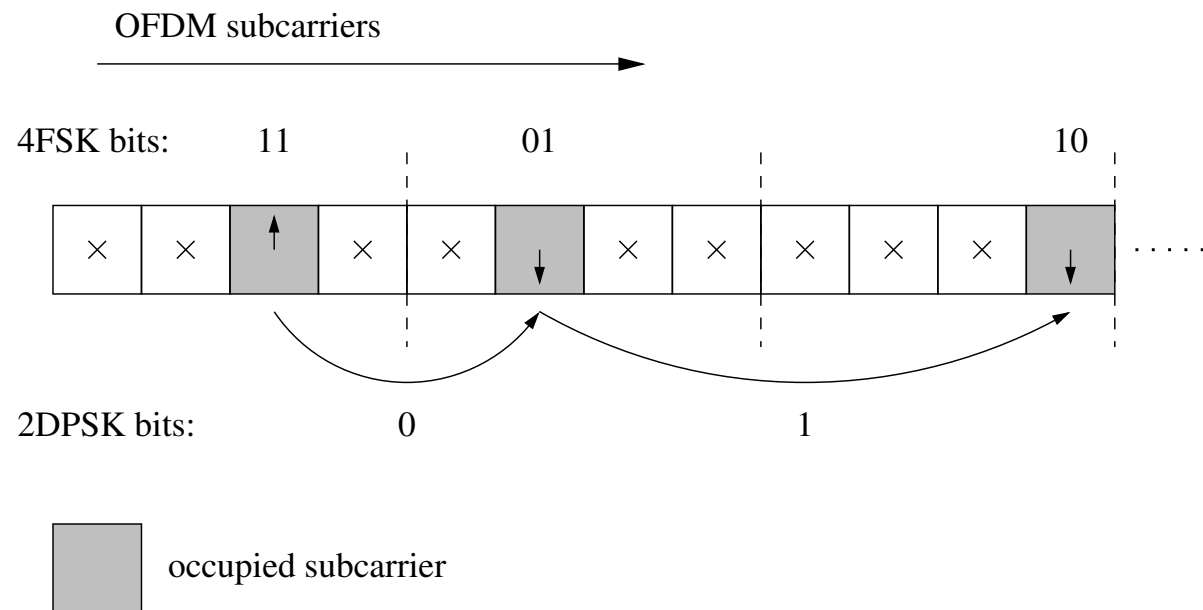
- ◆ Subcarrier phase of transmit symbols is arbitrary

This degree of freedom can be exploited

- ◆ Use phases to increase bandwidth efficiency by transmitting additional data
- ◆ Phases can be used for PAPR reduction
- ◆ Noncoherent detection of OFDM-MFSK is not influenced



## Hybrid Modulation Scheme



- ◆ Additional differential encoding of phases of occupied subcarriers
- ◆ Encoding in frequency or time direction
- ◆ Noncoherent detection, no CSI needed



## Channel Coding

- ◆ Separate encoding of MFSK and DPSK component
- ◆ Detection and decoding of MFSK component first to determine occupied subcarriers
- ◆ Afterwards detection and decoding of DPSK component

### Advantages:

- ◆ Different level of protection for both components using different codes
- ◆ Coded OFDM-MFSK transmission is not affected by DPSK component

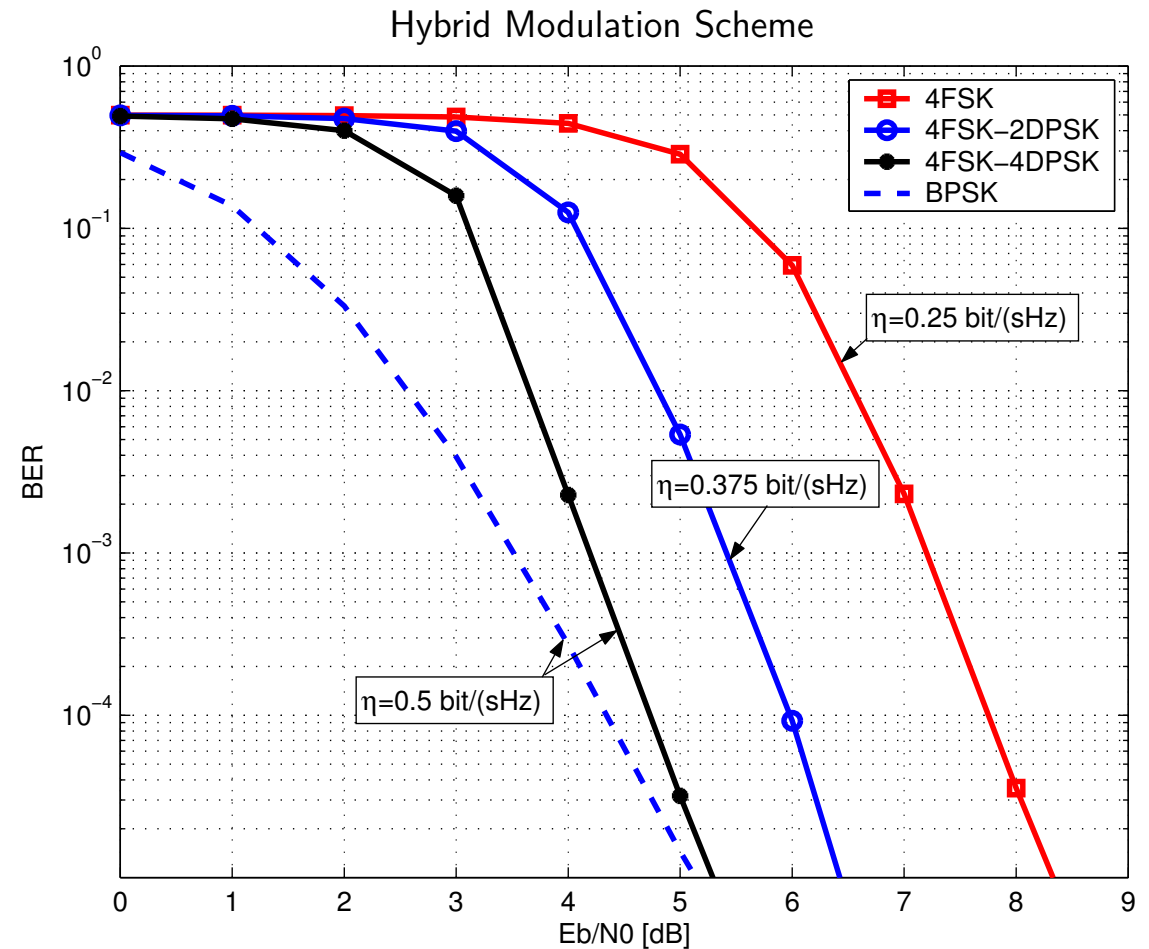
Convolutional code: rate  $1/2$ , memory 6, generator polynomial  $[133,171]$ ,  
soft decision detection



## Simulation Results – AWGN

Overall BER for coded transmission:

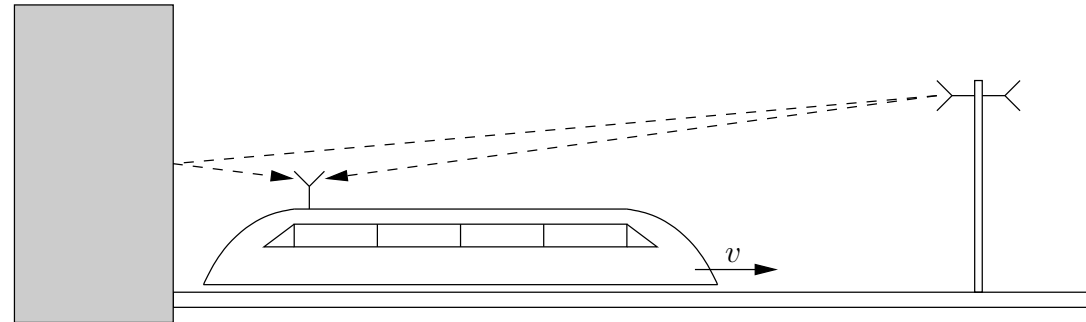
- ◆ Separate coding for 4FSK and DPSK component using the same convolutional code
- ◆ BER is dominated by 4FSK errors for AWGN
- ◆ Codes can be adapted







## Worst Case Channel Model



- ◆ Reflection at tunnel entrance or bridge
- ◆ Two paths with equal attenuation
- ◆ Maximum Doppler spread  $2f_d = 2f_c \frac{v}{c}$  due to opposite direction of arrival

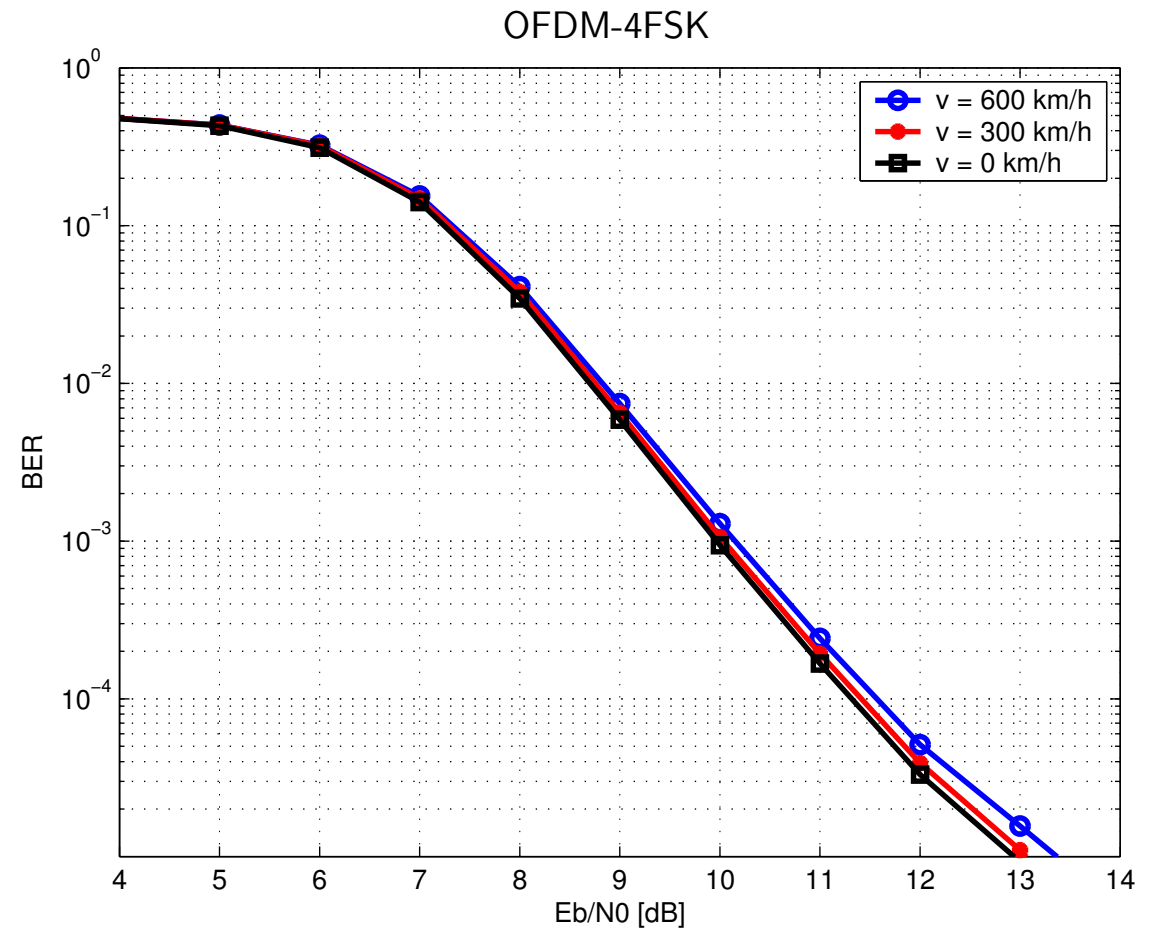
carrier frequency	$f_c = 38 \text{ GHz}$	subcarrier separation	$\Delta f = 312.5 \text{ kHz}$
FFT length	$N_f = 256$	cyclic extension	$T_g = N_g \Delta t = 0.8 \mu\text{s}$
no. of used subcarriers	$N_{f_{\text{used}}} = 160$	symbol duration	$T_s = (N_g + N_f) \Delta t = 4 \mu\text{s}$



## Simulation Results

BER for coded OFDM-4FSK:

- ◆ Path delay  $t_d = 0.75 \mu s$
- ◆ Strong frequency selectivity
- ◆ Very robust against frequency selectivity
- ◆ Very robust against high velocity

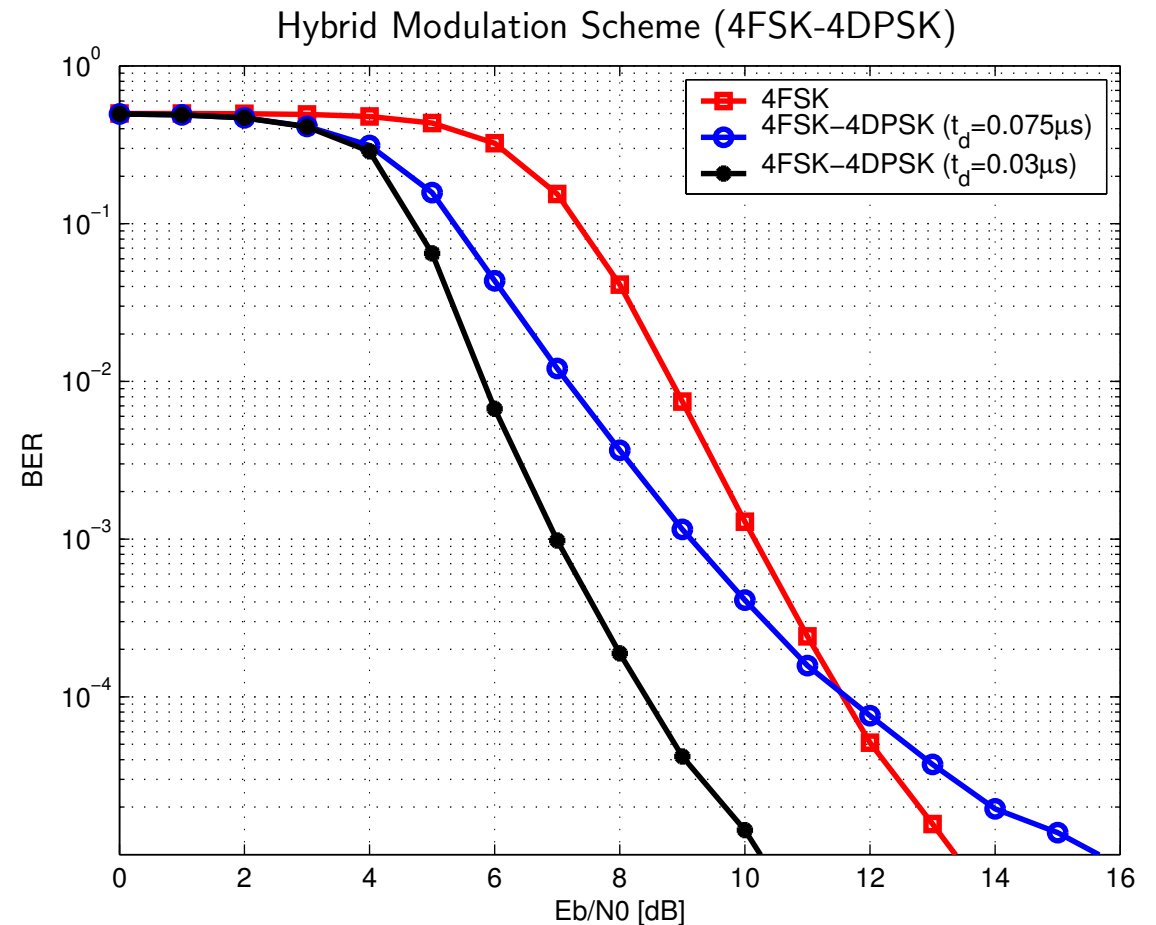




## Simulation Results

Overall BER for coded transmission:

- ◆ DPSK component encoded in frequency direction
- ◆ Speed  $v = 600 \text{ km/h}$
- ◆ Very robust against high velocity
- ◆ DPSK component very sensitive against frequency selectivity (large distance between used subcarriers)





## The PAPR Problem

Definition of the PAPR:

$$PAPR = \frac{(\max_t |s(t)|)^2}{\frac{1}{T_s} \int_0^{T_s} |s(t)|^2 dt}$$

- ◆ Unfavourable superposition of subcarriers in OFDM may lead to high PAPR
- ◆ Problem: Transmit amplifier has saturation limit
  - ✗ Nonlinear distortion (out of band radiation)
  - ✗ High backoff necessary (amplifier inefficient)
- ◆ Noncoherently detected OFDM-MFSK:
  - ✗ Subcarrier phases can be chosen arbitrarily so that PAPR is reduced
  - ✗ No side information necessary



## The PAPR Problem

Goal: Find optimum subcarrier phases for each OFDM symbol, so that PAPR is minimum

Problem:  $N = 256$  and OFDM-4FSK:

- ◆  $2^{128}$  possible OFDM symbols

- ◆  $2^{64}$  possibilities to assign the phase if only two phases for each subcarrier are considered

⇒ Exhaustive search is impossible

Worst case: All subcarrier phases are the same

- ◆ Subcarriers add coherently

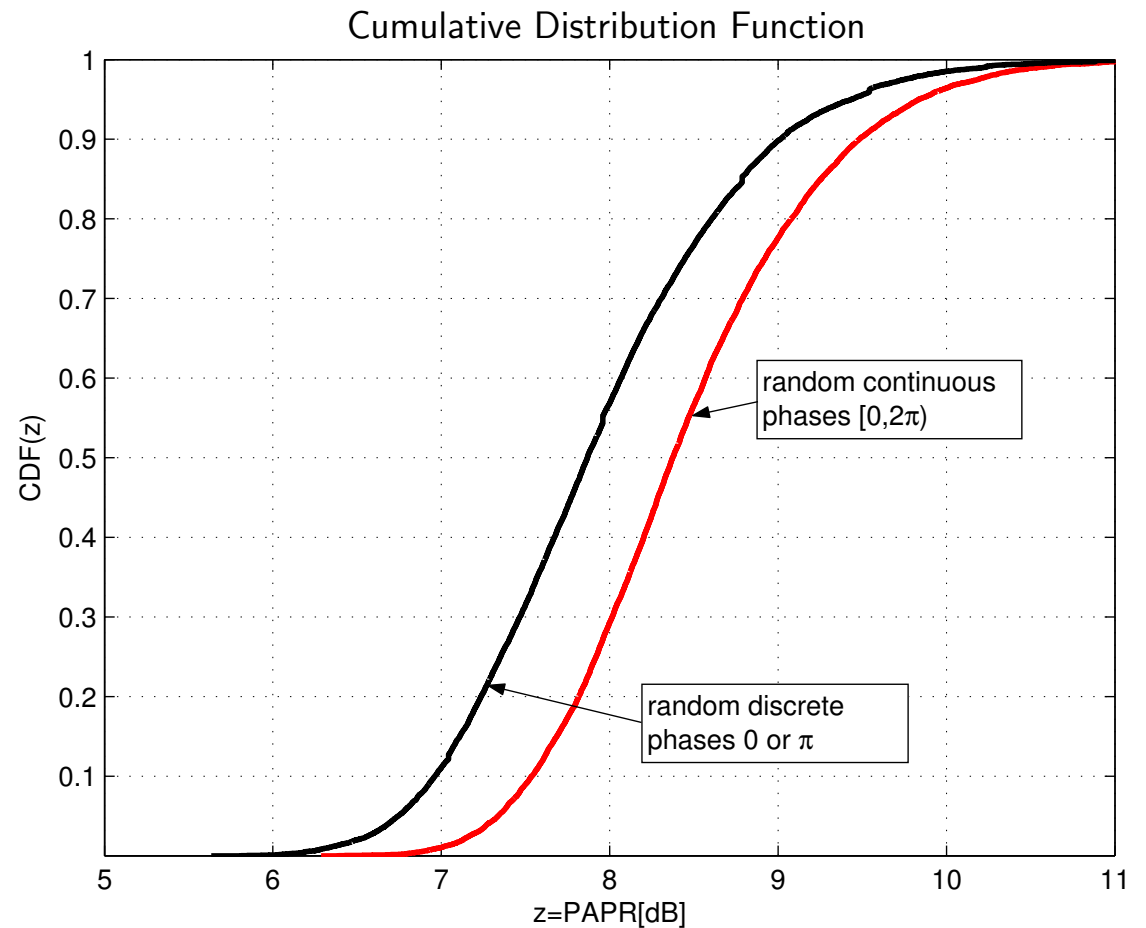
- ◆  $\text{PAPR} = \frac{N}{M} = \frac{256}{4} = 18 \text{ dB}$



## PAPR Distribution – Random Phases

First Approach:

- ◆ Use random phases
- ◆ Allow only binary phases
- ◆ No additional complexity

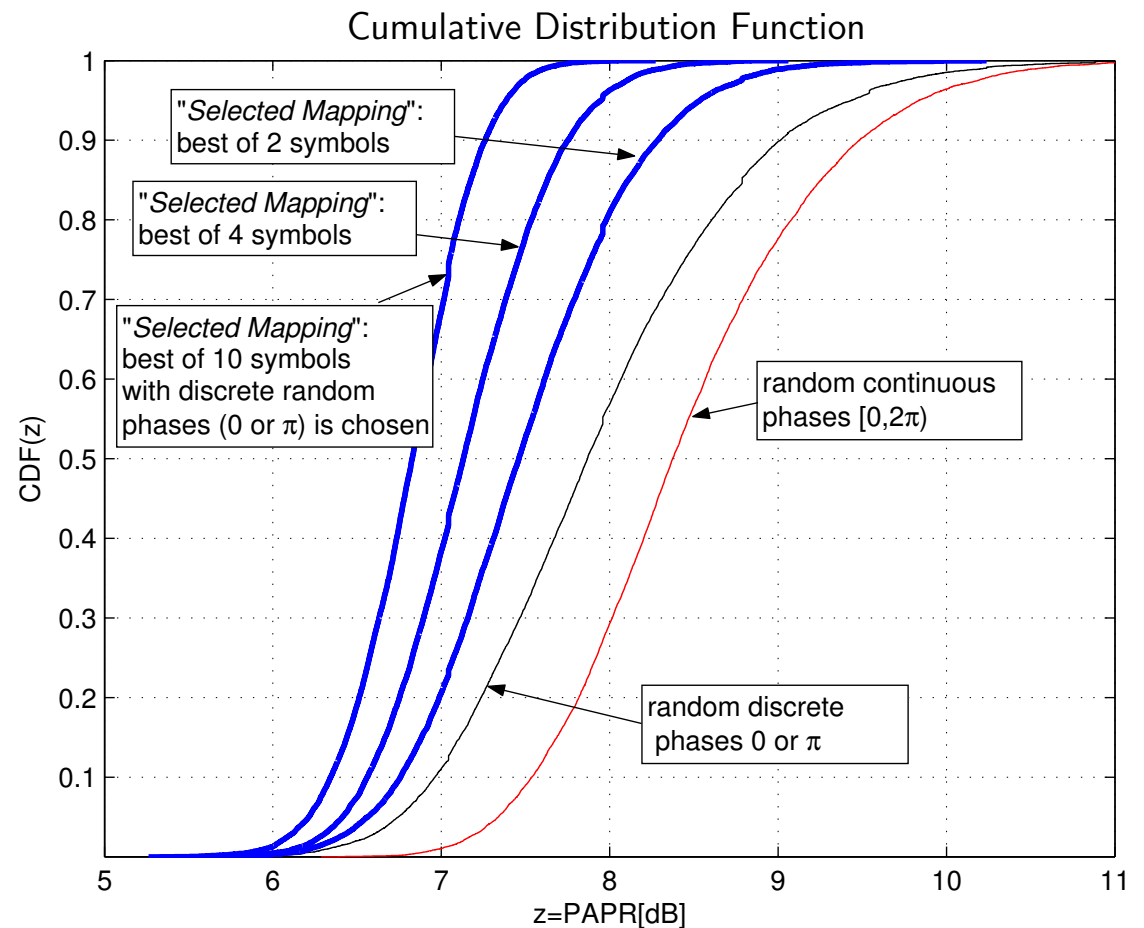




## PAPR Distribution - Selected Mapping

### Selected Mapping:

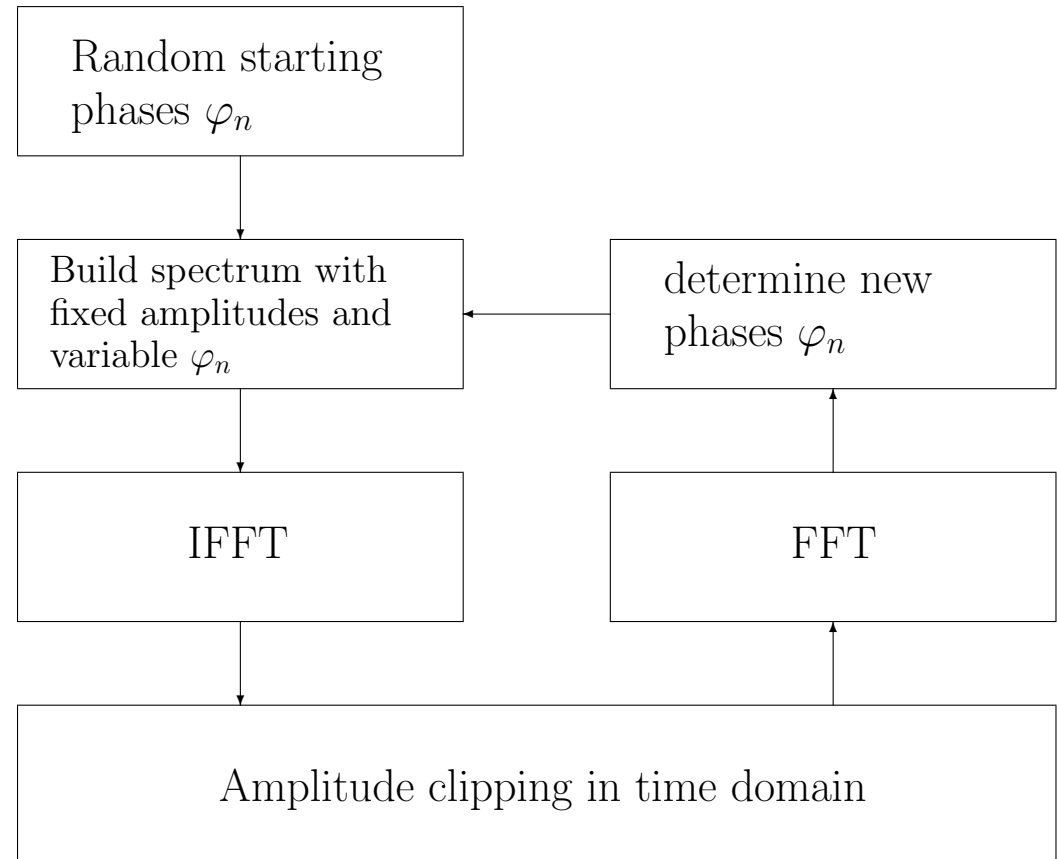
- ◆ Introduced by Bäuml, Huber and Fischer ('96)
- ◆ Assign random phases to each symbol several times
- ◆ Select OFDM symbol with lowest PAPR for transmission
- ◆ For noncoherently detected OFDM-MFSK no side information is needed





## Time-Frequency Domain Swapping

- ◆ Introduced by Ouderaa et al. ('88)
- ◆ Swapping between time and frequency domain
- ◆ Iterative reduction of PAPR
- ◆ Stop when PAPR is not decreasing any more
- ◆ Parameter: time domain clipping level CL

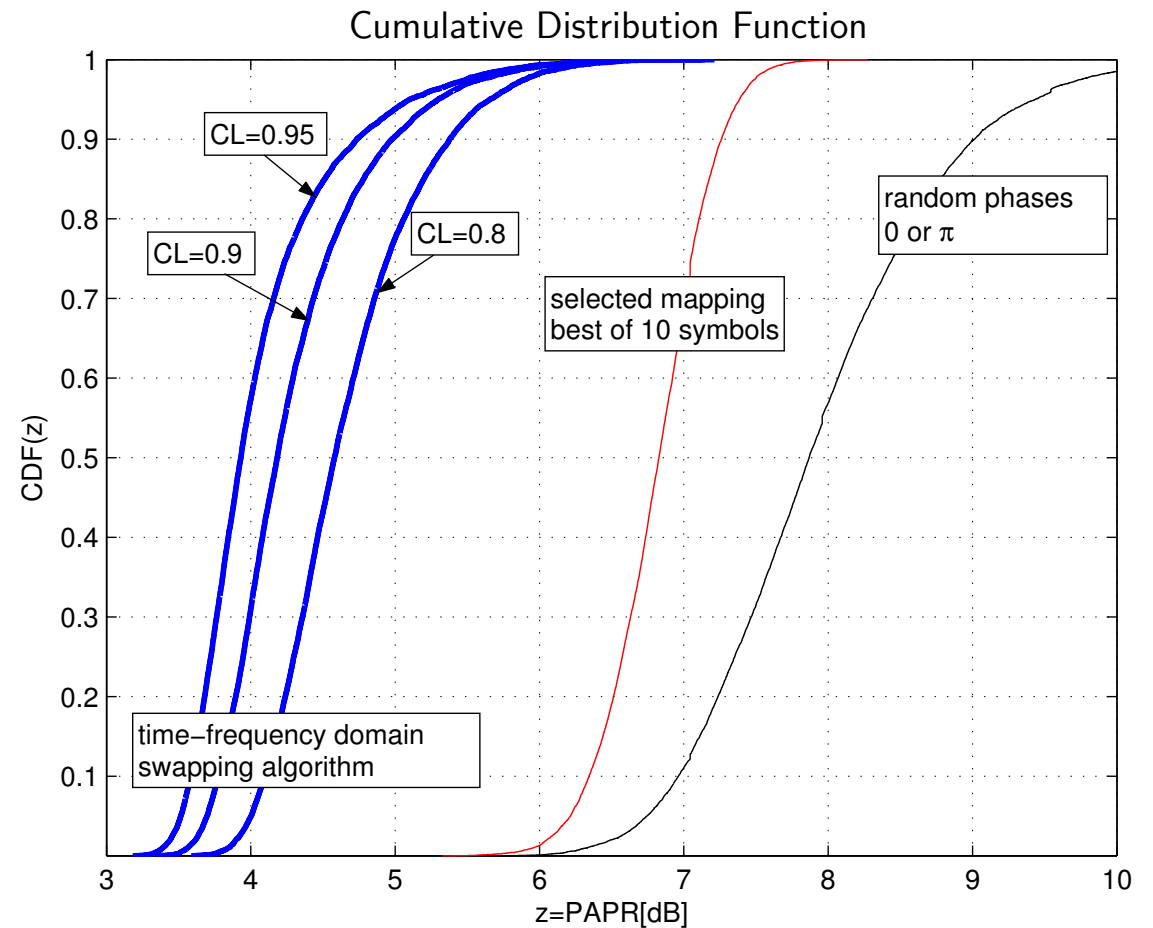






## PAPR Distribution - Swapping Algorithm

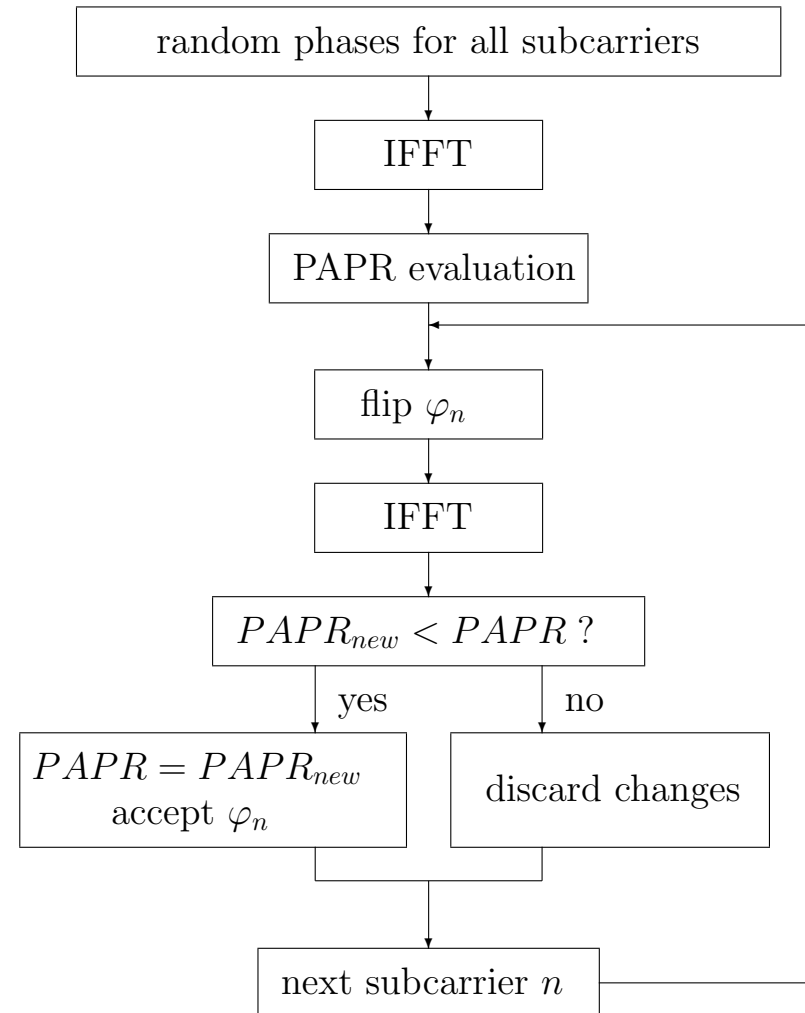
- ◆ Good performance
- ◆ Very high complexity: up to several hundred iterations per symbol





## Sequential Algorithm

- ◆ Subcarrier phases are systematically changed to reduce PAPR
- ◆ Subcarrier phases are flipped sequentially
- ◆ Complexity: one extra IFFT per occupied subcarrier
- ◆ Complexity can be reduced by exploiting linearity of DFT

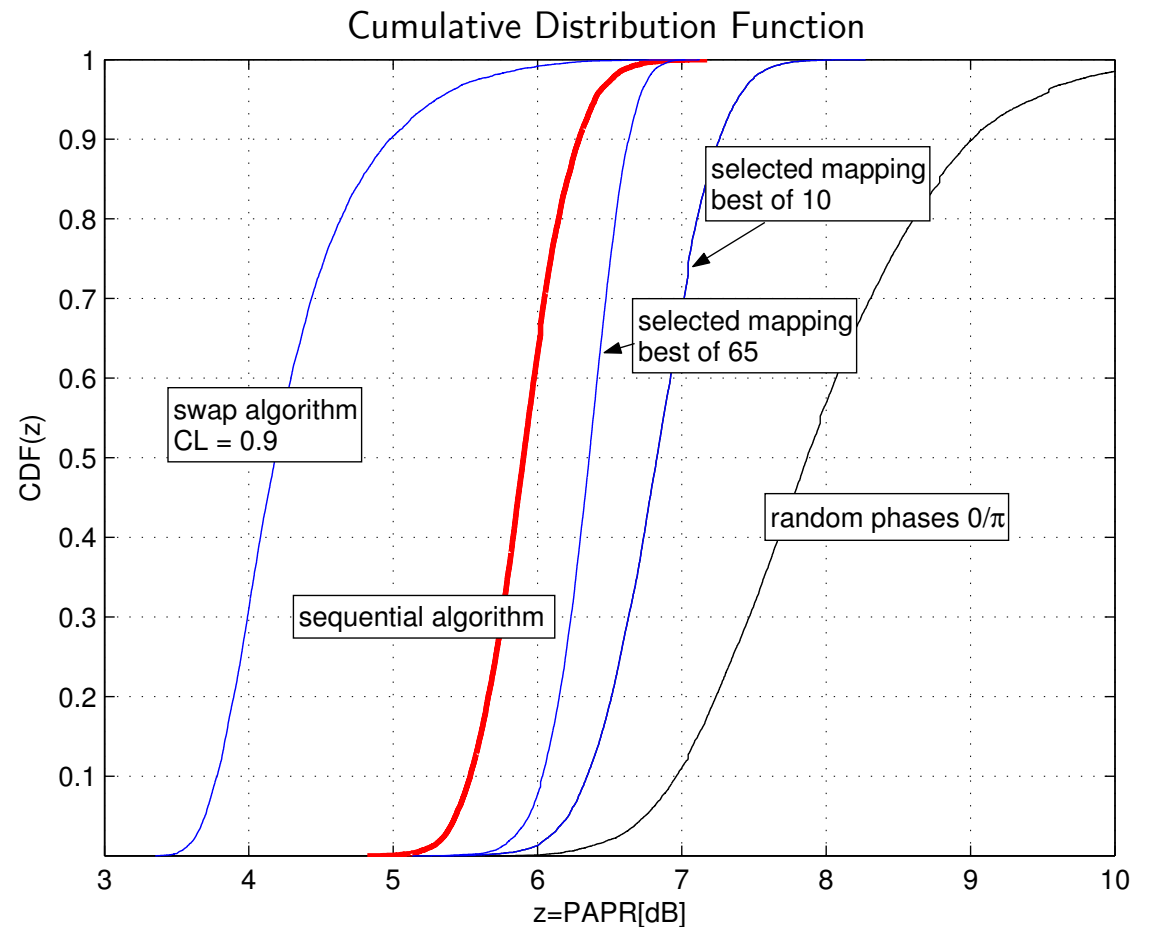




## PAPR Distribution - Sequential Algorithm

- ◆ Better performance than selected mapping
- ◆ Lower complexity than swapping algorithm

Good complexity/performance tradeoff





## Conclusions

- ◆ Noncoherently detected OFDM-MFSK is a robust transmission scheme in fast fading environments
- ◆ Subcarrier phases can be used for PAPR reduction or transmission of additional data
- ◆ Hybrid modulation does not affect the underlying MFSK transmission but offers additional data rate for moderate channels
- ◆ no CSI necessary
- ◆ PAPR reduction methods do not affect the noncoherent MFSK detection but reduce the PAPR
- ◆ In general: the better the performance of PAPR reduction methods the higher the complexity





## CDF - QPSK vs. BPSK

Assumption:

all subcarriers occupied, QPSK modulation (or random phases  $\varphi_n \in [0, 2\pi)$ ), no oversampling

All  $N_f$  time domain samples are Gaussian distributed and uncorrelated:

$$P(\text{PAPR} \leq z) = CDF(z) = (1 - e^{-z})^{N_f} \quad (1)$$

On the other hand, if we allow only  $\varphi_n \in \{0, \pi\}$ , i.e. the OFDM symbols in the frequency domain are real-valued, some of the time domain samples will be correlated:

$$P(\text{PAPR} \leq z) = (1 - \text{erfc}(\sqrt{z/2}))^2 (1 - e^{-z})^{\frac{N_f-2}{2}} \quad (2)$$